

Let $\phi_{1s}(r) = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0}$ be 1-s hydrogen orbital.

Wave function of e-p system is

$$f(\vec{x}, \vec{y}, t) = e^{-iEt} \phi_{1s}(|\vec{x} - \vec{y}|) e^{i\vec{P} \cdot \vec{r}_{cm}},$$

where

$$\vec{r}_{cm} = \frac{m_e \vec{x} + m_p \vec{y}}{m_e + m_p}$$

$$E = \frac{P^2}{2(m_e + m_p)} - E_0,$$

where $E_0 =$ binding energy of 1-s state.

$$|f\rangle = \int d^3x \int d^3y \psi_e^\dagger(\vec{x}, t) \psi_p^\dagger(\vec{y}, t) |0\rangle f(\vec{x}, \vec{y}, t).$$

No symmetrization is needed since the particles are distinguishable. A normalization integral involves

$$\begin{aligned} & \langle 0 | \psi_p(\vec{y}, t) \psi_e(\vec{x}, t) \psi_e^\dagger(\vec{x}', t) \psi_p^\dagger(\vec{y}', t) | 0 \rangle \\ &= \langle 0 | \psi_p(\vec{y}, t) \{ \psi_e(\vec{x}, t), \psi_e^\dagger(\vec{x}', t) \} \psi_p^\dagger(\vec{y}', t) | 0 \rangle \\ &+ \langle 0 | \psi_p(\vec{y}, t) \psi_e^\dagger(\vec{x}', t) \psi_p^\dagger(\vec{y}', t) \psi_e(\vec{x}, t) | 0 \rangle \end{aligned}$$

(since ψ_e & ψ_p anticommute at equal time).

$$\begin{aligned} &= \delta^{(3)}(\vec{x} - \vec{x}') \langle 0 | \psi_p(\vec{y}, t) \psi_p^\dagger(\vec{y}', t) | 0 \rangle + 0 \\ &= \delta^{(3)}(\vec{x} - \vec{x}') \delta^{(3)}(\vec{y} - \vec{y}'). \end{aligned}$$

There is no δ -fn between $\vec{x} \otimes \vec{y}'$ or $\vec{y} \otimes \vec{x}'$, since fields for different types of particles (anti)commute.